# Pumping effect due to gas evolution in flow-through electrolysers

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In electrolysers with recirculation where a gas is evolved, the pumping of electrolyte from a lower to a higher level can be effected by the air-lift effect due to the difference between the densities of the inlet electrolyte and the gaseous dispersion at the outlet. A balance equation for calculation of the rate of flow of the pumped liquid is derived. An equation for the calculation of the mean volume fraction of bubbles in the space between the electrodes is proposed and verified experimentally on a pilot electrolyser. The pumping efficiency of the air-lift effect is determined.

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### Nomenclature

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		$l_{\rm v}, l_{\rm s}$	length of tubing, see Fig. 1 (m)
$a'_{\rm A}, a'_{\rm C}$	constants of linearized Tafel	$n_{O_2}, n_{H_2}$	number of electrons transferred per
	Equation 7 (V)	02 m2	molecule of $O_2$ or $H_2$
b	electrode width (m)	$N_{\rm B}, N_{\rm E}$	pumping power, pumping 'extra-
$b'_{\rm A},  b'_{\rm C}$	constants of linearized Tafel		power', Equations 28, 31 (W)
	Equation 7 $(Vm^{-2}A^{-1})$	$N_{ m T}$	total power input for electrolysis
$c_{\rm pE}$	specific heat of electrolyte $(J kg^{-1})$		(W)
•	K <sup>-1</sup> )	$\Delta p_{\rm M}, \Delta p_{\rm p},$	pressure losses in the interelectrode
d	interelectrode distance (m)	$\Delta p_z$	space, in the inlet tubing and in
$d_{\rm E}$	equivalent diameter of interelec-		elbows $(Nm^{-2})$
	trode space (m)	Р	pressure at the upper edge of the
$d_{\mathrm{T}}$	diameter of tubing (m)		electrode $(N m^{-2})$
$E_{\rm A}, E_{\rm C}$	potential of anode and cathode (V)	R	gas constant $(JK^{-1}mol^{-1})$
f	correction term, see Equation 11	Re, Re <sub>M</sub>	Reynolds criterion for the elec-
F	Faraday's constant (96 484 C mol <sup><math>-1</math></sup> )		trolyte and for gas dispersion
g	acceleration of gravity $(9.81 \text{ m s}^{-2})$	$S_{\rm A}, S_{\rm C}$	thickness of anode and cathode (m)
$H_{-}$	function defined by Equation 16	Т	temperature (K)
I <sub>T</sub>	total current flowing through elec-	$T_0, T_T$	temperatures at the inlet and outlet
	trolyser (A)		(K)
j	local current density $(A m^{-2})$	$\Delta T$	temperature difference, $T_T - T_0$
Ī	mean current density $(A m^{-2})$		(K)
$j_{\zeta}$	reduced local current density	U	terminal voltage of electrolyser (V)
$K_1, K_{2B}$	criteria defined by Equations 12	$\Delta U$	increase of the mean voltage drop
	and 13		in the interelectrode space due to
$K_3$	criterion defined by Equation 9		presence of bubbles (V)
$\Delta l$	pumping height equal to $l_{\rm E} - l_{\rm T}$ (m)	$v_{\rm E}, v_{\rm M}$	velocities of electrolyte and of
$l_{\rm E}$	electrode height (m)		gas dispersion between electrodes
l <sub>H</sub>	length of tubing above electrolyser		$(m s^{-1})$
	(m)	$v_{p}$	velocity of electrolyte in inlet

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level height in reservoir (m)

	channel (m s $^{-1}$ )	$Q_{\rm E}, Q_{\rm M}$	density of electrolyte and gas dis-
$v_{R}$	rising velocity of bubbles $(m s^{-1})$		persion $(kg m^{-3})$
$\dot{V}_{ m E}$	volume rate of flow of electrolyte $(m^3 s^{-1})$	$\mu_{\rm E},\mu_{\rm M}$	dynamic viscosity of electrolyte and gas dispersion $(kg m^{-1} s^{-1})$
$\dot{V}_{\rm G}(x)$	volume rate of flow of gas at height $x \text{ (m}^3 \text{ s}^{-1})$	$\mu_0$	dynamic viscosity of electrolyte at inlet temperature $(kg m^{-1} s^{-1})$
$\dot{V}_{ m GT}$	volume rate of flow of gas at upper electrode edge $(m^3 s^{-1})$	λ	friction coefficient of electrolyte in a tube
x	distance from lower electrode edge (m)	$\lambda_{M}$	friction coefficient of gas dispersion between electrodes
$\alpha(x), \ \overline{\alpha}$	volume fraction of bubbles at height x between electrodes, and its mean value (Equations 5a, 22a)	$\eta_{\mathrm{P}} \ \eta_{\mathrm{O}_2}, \ \eta_{\mathrm{H}_2}$	pump efficiency (%) current efficiency for oxygen and hydrogen
$\alpha_{\rm T}$	volume fractions of bubbles at upper electrode edge of electrolyte	$\xi \Delta E_{ m pot}$	reduced height coordinate, $x/l_{\rm E}$ volume-specific potential energy dif-
$\alpha_{\infty}$	maximum volume fraction of bubbles	$\Delta E_{\rm kin}$	ference of electrolyte $(J m^{-3})$ volume-specific kinetic energy dif-
χ <sub>Α</sub> , χ <sub>C</sub> , χ <sub>E</sub> , χ <sub>M</sub>	specific electric conductivity of anode, cathode, electrolyte and gas dispersion $(\Omega^{-1}m^{-1})$	$\Delta E_{ m dis}$	terence of electrolyte $(J m^{-3})$ volume-specific dissipated energy of electrolyte $(J m^{-3})$

#### 1. Introduction

In technical practice, circulation of electrolyte between a reservoir or reactor and the electrolyser proper is effected by means of a pump placed in the connecting tube. If a gas is evolved in the electrolyser it is possible to arrange that the gas dispersion (with a lower density) streams into the reservoir while the solution from the reservoir (without the gas bubbles) passes into the electrolyser. This principle is utilized in water electrolysis [1] and in electro-chemical production of chlorates [2], etc. If high rates of flow are not required, the principle is energetically acceptable and it operates reliably since there are no moving parts and no maintenance problems. For high rates of flow or large pumping height, pumping by the gas-lift effect is energetically too expensive.

#### 2. Theoretical considerations

The calculation of the pumping rate is based on a pressure balance in the corresponding hydraulic circuit [3, 4] (Fig. 1). Bubbles are formed in the interelectrode space so that the mean relative content of the gas phase in a part of the circuit of height  $l_E$  is equal to  $\bar{\alpha}$ . In a part of the tubing at a height  $l_E$  above the electrolyser, the mean content of the gas phase is equal to  $\alpha_T$ , which is higher than  $\bar{\alpha}$ . The electrolyte in the separator and in the connecting pipe of height  $l_T$  is without bubbles. Circulation of the electrolyte is caused by a difference between the density of the electrolyte at the inlet and that of the electrolyte in part of the electrolyser. The power consumed per unit volume of the flowing electrolyte (W s m<sup>-3</sup> or J m<sup>-3</sup>) is changed irreversibly to heat by friction; any heat evolved in the system is conducted to the surroundings so that the system can be considered approximately isothermal.

Let us choose two levels, 1–1 and 2–2 (Fig. 1), at which the balance of the specific (volume) kinetic and potential energies are made. Then

$$\Delta E_{\text{pot}} = g \varrho_{\text{E}} l_{\text{T}} - \varrho_{\text{E}} l_{\text{E}} (1 - \tilde{\alpha}) - g \varrho_{\text{E}} l_{\text{H}} (1 - \alpha_{\text{T}})$$
(1a)

$$\Delta E_{\rm kin} = \frac{1}{2} \varrho_{\rm E} (\dot{V}_{\rm E}/F_{11})^2 - \frac{1}{2} \varrho_{\rm E} (1 - \alpha_{\rm T})^{-1} (\dot{V}_{\rm E}/F_{22})^2$$
(1b)

$$\Delta E_{\rm dis} = \Delta p_{\rm M} + \Delta p_{\rm p} + \Delta p_{\rm z} \tag{1c}$$



Fig. 1. Scheme of electrolyser with reservoir with electrolyte circulation caused by the formation of gas bubbles.  $l_{\rm E}$ , Electrode height;  $l_{\rm H}$ , vertical part of outlet tubing;  $l_{\rm D}$ , vertical part of inlet tubing;  $l_{\rm v}$ ,  $l_{\rm s}$ , length of connecting tubing at the outlet and inlet, respectively;  $l_{\rm T}$ , height of inlet tubing (reactor) filled with electrolyte; *E*, electrolyser; *R*, separator. Direction of flow is denoted by arrows.

The second term in Equation 1a involves the mean volume fraction of bubbles,  $\bar{\alpha}$ , and the third term involves the volume fraction of bubbles at the top of the electrolyser,  $\alpha_T$ . The cross-sectional areas of flow at the levels 1–1 and 2–2 are denoted as  $F_{11}$  and  $F_{22}$ . It should be noted that for closed systems the planes 1–1 and 2–2 should fuse to a single plane. For a closed system we usually presume that  $\Delta E_{kin}$  in the separator is zero, i.e. is dissipated as heat.

The terms in Equation 1c correspond to losses due to friction in the section containing a mixture of the gas and electrolyte  $(\Delta p_M)$  or electrolyte only  $(\Delta p_p)$ , and energy dissipated in places where the shape of the tube changes  $(\Delta p_z)$ .

The above equations can be combined to give

$$g\varrho_{\rm E}l_{\rm T} - g\varrho_{\rm E}l_{\rm E}(1-\bar{\alpha}) - g\varrho_{\rm E}l_{\rm H}(1-\alpha_{\rm T}) = \Delta p_{\rm M} + \Delta p_{\rm p} + \Delta p_{\rm z} + \frac{1}{2}\varrho_{\rm E}\left[\frac{(\dot{V}_{\rm E}/F_{22})^2}{1-\alpha_{\rm T}} - \left(\frac{\dot{V}_{\rm E}}{F_{11}}\right)^2\right]$$
(1d)

The basic physical parameters for the gas dispersion with a bubble volume fraction,  $\alpha$ , are given as

$$\varrho_{\rm M} = \varrho_{\rm E}(1-\alpha) \tag{2a}$$

$$\mu_{\rm M} = \mu_{\rm E} (1 - \alpha)^{-2.5} \tag{2b}$$

$$v_{\rm E} = \frac{\dot{V}_{\rm E}}{wd} \left[ \frac{1}{1 - \alpha(x)} \right]$$
(2c)

$$v_{\rm G} = \frac{\dot{V}_{\rm G}(x)}{wd} \left[ \frac{1}{\alpha(x)} \right]$$
(2d)

$$v_{\rm G} = v_{\rm E} + v_{\rm R} [1 - \alpha(x)]^{3.5}$$
 (2e)

The expressions for the dynamic viscosity,  $\mu_M$ , in Equation 2b and for the velocity of gas bubbles,  $v_G$ , in Equation 2e are discussed in [5]. In real dispersions containing spherical bubbles the volume fraction,  $\alpha(x)$ , cannot reach unity volume fraction. In a cubical arrangement the maximal volume gas fraction,  $\alpha_{\infty}$ , is 0.5236 and for the closest packing  $\alpha_{\infty} = 0.7408$ . For random packing a mean

value of  $\alpha_{\infty} = 0.63$  was predicted and corresponds to the stochastic frequency maximum [6]. Kreysa and Kuhn [7] slightly rearranged Equation 2e, introducing  $\alpha_{\infty}$ :

$$v_{\rm G} = v_{\rm E} + v_{\rm R} [1 - \alpha(x)]^{4.5} [1 - \alpha(x)/\alpha_{\infty}]^{-1}$$
(2f)

The velocity of rising bubbles relative to the moving electrolyte,  $v_{\rm R}$ , depends on the superficial gas velocity,  $\dot{V}_{\rm GT}/db$  [8], e.g. the bubble diameter is changed with the change of  $\dot{V}_{\rm GT}/bd$ . The corresponding Reynolds number is given as

$$Re_{\rm M} = \frac{\dot{V}_{\rm E} d_{\rm E} \varrho_{\rm E}}{b d \mu_{\rm E}} (1 - \alpha)^{2.5} = Re (1 - \alpha)^{2.5}$$
(3a)

where  $d_{\rm E}$  is the equivalent channel diameter,

$$d_{\rm E} = 2bd/(b+d) \tag{3b}$$

Here, b denotes electrode width and d denotes interelectrode distance. In practice,  $b \ge d$ .

The pressure losses in the interelectrode space can be calculated as

$$\Delta p_{\rm M} = \lambda_{\rm M} (l_{\rm E}/2d_{\rm E}) \varrho_{\rm E} (\dot{V}_{\rm E}/bd)^2 (1 - \bar{\alpha})^{-1}$$
(4a)

where

$$\lambda_{\rm M} = 96/Re_{\rm M} \quad \text{for} \quad Re_{\rm M} < 2300 \tag{4b}$$

$$\lambda_{\rm M} = 0.314/Re_{\rm M}^{0.25}$$
 for  $Re_{\rm M} > 2300$  (4c)

Analogous equations apply for  $\Delta p_p$ . For  $\Delta p_z$ , the term  $l_E/d_E$  is set equal to the value found in tables [9]. For example, for a change in direction at a right angle, this term lies between 30 and 70.

The volume fraction of bubbles at a height x, can be expressed, using Equations 2c, 2d and 2f, as

$$\alpha(x) = \dot{V}_{\rm G}(x)\alpha_{\infty}/\{\dot{V}_{\rm G}(x) + [\dot{V}_{\rm G}(x) + \dot{V}_{\rm E}] [\alpha_{\infty} - \alpha(x)] + \alpha_{\infty} b dv_{\rm R} [1 - \alpha(x)]^{5.5}\}$$
(5a)

where  $v_{\rm R}$  represents the velocity of rising bubbles relative to the moving electrolyte due to buoyancy.

The volume fraction of bubbles at the top of the electrolyser can be expressed as

$$\alpha_{\rm T} = \alpha_{\infty} \dot{V}_{\rm GT} / [\dot{V}_{\rm GT} + (\dot{V}_{\rm GT} + \dot{V}_{\rm E}) (\alpha_{\infty} - \alpha_{\rm T}) + \alpha_{\infty} b dv_{\rm R} (1 - \alpha_{\rm T})^{5.5}]$$
(5b)

The mean volume fraction of bubbles is given by

U

$$\bar{\alpha} = \int_0^1 \alpha(\xi) \ d\xi \tag{5c}$$

It was assumed [3] that  $\bar{\alpha}/\alpha_{\rm T} = 0.5$ , corresponding to current densities being independent of x. It will be shown that this simplification is possible if  $\alpha_{\rm T} \rightarrow 0$ , whereas in the general case of uneven current density distribution along the height of the electrolyser,  $\bar{\alpha}/\alpha_{\rm T} > 0.5$ .

#### 2.1. Analytical calculation of $\bar{\alpha}/\alpha_{\rm T}$ for a bipolar electrolyser neglecting the velocity of rising bubbles

The equation for the voltage drop along a current line at height  $\xi$  in a bipolar electrolyser reads

$$= a'_{A} + b'_{A}j(\xi) + a'_{C} + b'_{C}j(\xi) + j(\xi) [S_{A}\chi_{A}^{-1} + S_{C}\chi_{C}^{-1}] + j(\xi) d\chi_{E}^{-1} \left[ 1 + 1.5K_{3}f \int_{0}^{\xi} \frac{j(\xi)}{j} d\xi \right]$$
(6)

This gives the terminal voltage, U, of the electrolyser. The first four terms on the right-hand side correspond to the anode and cathode potentials.

$$E_{\rm A} = a'_{\rm A} + b'_{\rm A} j(\xi) \tag{7a}$$

$$-E_{\rm C} = a_{\rm C}' + b_{\rm C}' j(\xi) \tag{7b}$$

Equations 7a and 7b are justified only for small deviations of  $j(\xi)$  about  $\overline{j}$ .

Then comes the voltage drop in the anode and cathode of thickness  $S_A$  and  $S_C$  and specific conductivity  $\chi_A$  and  $\chi_C$ , respectively. The last term represents the voltage drop in the space between the electrodes, where the specific resistivity of the gas dispersion is given by the Maxwell equation [3, 12], Equation 8a. There are also other equations for the calculation of  $\chi_M$  [10, 11], but the Maxwell equation leads to an analytical solution. It is worth mentioning that the Maxwell equation slightly underestimates  $\chi_M^{-1}$  so that a more uniform current density distribution is eventually obtained. Hence, for a flow-through system

$$\chi_{\rm M}^{-1} = \chi_{\rm E}^{-1} \left\{ 1 + 1.5 \left[ \frac{\dot{V}_{\rm G}(x)}{\dot{V}_{\rm E}} \right] \left[ \frac{v_{\rm E}(x)}{v_{\rm G}(x)} \right] \right\}$$
(8a)

$$\chi_{\rm M}^{-1} = \chi_{\rm E}^{-1} \left[ 1 + 1.5 K_3 f \int_0^{\xi} \frac{j(\xi)}{\bar{j}} d\xi \right]$$
(8b)

where

$$\frac{\dot{V}_{\rm G}(x)}{\dot{V}_{\rm GT}} = \int_0^{\xi} \frac{j(\xi)}{\bar{j}} d\xi \tag{9}$$

and

$$K_3 = \frac{\alpha_{\rm T}}{1 - \alpha_{\rm T}} \tag{10}$$

$$f = [\dot{V}_{\rm E} + b dv_{\rm R} (1 - \alpha_{\rm T})^{5.5} (1 - \alpha_{\rm T}/\alpha_{\infty})^{-1}] / [\dot{V}_{\rm E} + b dv_{\rm R} (1 - \alpha(x))^{5.5} (1 - \alpha(x)/\alpha_{\infty})^{-1}]$$
(11)

Equation 8 is strictly valid only if  $\alpha_T < 0.2$ , whereas for higher values of  $\alpha_T$  the specific electric resistivity of the dispersion is better expressed by the Bruggeman equation [10]

$$\chi_{\rm M}^{-1} = \chi_{\rm E}^{-1} \left[ 1 + K_3 f \int_0^{\xi} \frac{j(\xi)}{\bar{j}} d\xi \right]^{1.5}$$
(12)

Since we want to obtain an analytical solution, we use Equation 8 for  $v_{\rm R} = 0$  and for any values of  $\alpha_{\rm T}$ , taking into account that for higher values of  $\alpha_{\rm T}$  the calculated resistivity and the ratio of  $\alpha/\alpha_{\rm T}$  will be smaller than with the use of Equation 12.

Introducing dimensionless criteria and simplexes

$$j_{\xi} = j(\xi)/\overline{j} \tag{13b}$$

$$K_{1} = (U - a'_{\rm A} - a'_{\rm C})/\bar{j}d \chi_{\rm E}^{-1}$$
(13b)

$$K_{2B} = (b'_{A} + b'_{C})/d \chi_{E}^{-1} + (S_{A}\chi_{A}^{-1} + S_{C}\chi_{C}^{-1})/d \chi_{E}^{-1}$$
(13c)

Equation 6, which is now valid only for  $v_{\rm R} = 0$ , can be rearranged in the form

$$K_1 = K_{2B}j_{\xi} + j_{\xi}(1 + 1.5K_3 \int_0^{\xi} j_{\xi} d\xi)$$
(14)

The value of  $K_1$  (or U) is not known, but it can be calculated by using the equation for the current density balance

$$\int_{0}^{1} j_{\xi} d\xi = 1$$
 (15)

Equation 14 can be transformed by substituting

$$\int_0^{\xi} j_{\xi} d\xi = H \tag{16}$$

into the form

$$K_1 = K_{2B}H' + (1 + 1.5K_3H)H'$$
(17)

The boundary conditions are  $H(\xi = 0) = 0$ ,  $H(\xi = 1) = 1$ . Since the value of  $K_1$  is not known, two boundary conditions are needed; the latter follows from Equation 15. The solution leads to

$$K_1 = 1 + K_{2B} + 0.75K_3 \tag{18}$$

$$H(\xi) = [(3K_1K_3\xi + (1 + K_{2B})^2)^{\frac{1}{2}} - 1 - K_{2B}]/1.5K_3$$
(19)

$$H'(\xi) = j_{\xi} = K_1 (3K_1 K_3 \xi + (1 + K_{2B})^2)^{-\frac{1}{2}}$$
(20)

The following equation is important for further calculations:

$$H(\xi) = \int_0^{\xi} j_{\xi} d\xi = \dot{V}_{\rm G}(\xi) / \dot{V}_{\rm GT}$$
(21)

Equation 5c can be rearranged by using Equations 5a and 21 for  $v_{\rm R} = 0$  to the form

$$\bar{\alpha} = \int_{0}^{1} \frac{\dot{V}_{G}(\xi) d\xi}{\dot{V}_{E} + \dot{V}_{G}(\xi)} = \int_{0}^{1} \frac{H d\xi}{\dot{V}_{E} / \dot{V}_{GT} + H}$$
(22a)

From the definition of  $K_3$ , we then obtain

$$\frac{\tilde{\alpha}}{\alpha_{\rm T}} = (1 + K_3) \int_0^1 \frac{H d\xi}{1 + K_3 H}$$
(22b)

By substituting Equation 19 for H in Equation 22b and integrating we obtain the resulting equation for the volume fraction of bubbles

$$\bar{\alpha}/\alpha_{\rm T} = (1 + 1/K_3) \left\{ 1 - \left[ (3K_1K_3 + (1 + K_{2\rm B})^2)^{\frac{1}{2}} - 1 - K_{2\rm B} \right] / K_1K_3 + (K_{2\rm B} - 0.5) \ln \left[ ((3K_1K_3 + (1 + K_{2\rm B})^2)^{\frac{1}{2}} - K_{2\rm B} + 0.5) / 1.5 \right] \right\}$$
(23)

This equation shows that the ratio of  $\bar{\alpha}/\alpha_{\rm T}$  increases with the value of  $K_2$  ( $K_2$  increases with increasing  $b'_{\rm A}$  and  $b'_{\rm C}$  and decreasing  $d\chi_{\rm E}^{-1}$ ) and approaches 0.5 for  $K_3 \rightarrow 0$  (for low gas fractions).

In calculating the value of  $K_3$  we must know the value of  $\dot{V}_{GT}$  corresponding to the total current,  $I_T$ , flowing through the system. For example, for diaphragm-less water electrolysis in alkaline medium (such as was used in our experiments) we have

$$\dot{V}_{\rm GT} = \frac{I_{\rm T}}{F} \left( {}_{4}^{1} \eta_{\rm O_2} + {}_{2}^{1} \eta_{\rm H_2} \right) \frac{RT_{\rm T}}{P}$$
(24)

where  $\eta_{O_2} \leq 1$ ,  $\eta_{H_2} \leq 1$  and RT/P is the molar volume of the (ideal) gas at a pressure P and temperature  $T_T$  at the upper edge of the electrolyser electrodes.

#### 2.2. Numerical calculation of $\bar{\alpha}$ for one cell of a bipolar electrolyser

The voltage balance referring to a current line for a bipolar electrolyser using the Bruggeman equation 11 reads

$$U = a'_{\rm A} + b'_{\rm A}j_{\xi} + a'_{\rm C} + b'_{\rm C}j_{\xi} + j_{\xi}(S_{\rm A}\chi_{\rm A}^{-1} + S_{\rm C}\chi_{\rm C}^{-1}) + j_{\xi} d\chi_{\rm E}^{-1} \left(1 + K_{3}f \int_{0}^{\xi} \frac{j_{\xi}}{j} d\xi\right)^{1.5}$$
(25)

Equation 25 is valid for  $j(\xi) \approx \overline{j}$ ; for other cases we can use  $b_A \ln [j(\xi)]$  and  $b_C \ln [j(\xi)]$  for the



Fig. 2. Experimental set-up. 1, Reservoir with 200 litres 8.77% NaOH; 2, overflow to maintain the level; 3, one cell of bipolar electrolyser,  $13 \times 70$  cm; 4, overflow to reservoir, 5, for measurement of the rate of flow; 6, water gauge for reservoir 5; 7, reservoir with soda lye; 8, pump with controllable speed of revolution of electric motor, 9.  $l_{\rm T}$ , Level height in reservoir;  $l_{\rm E}$ , electrode height;  $\Delta l$ , pumping height.

electrode polarization instead of  $b'_{A}$  and  $b'_{C}$ . Equation 25 can be rearranged using dimensionless numbers and simplexes into the form

$$K_1 = K_{2B}j_{\xi} + j_{\xi} \left(1 + K_3 f \int_0^{\xi} j_{\xi} d\xi\right)^{1.5}$$
(26)

Equation 15 is to be used for the calculation of  $K_1$ . The value of  $\bar{\alpha}$  can be obtained by numerical integration of Equation 5c.

Using Equation 16 as the definition of H we have to solve Equation 27:

$$H' = \frac{K_1}{K_{2B} + (1 + K_3 fH)^{1.5}}$$
(27)

with boundary conditions H(0) = 0; H(1) = 1.

#### 2.3. Power loss due to pumping by the buoyancy effect of gas bubbles

We shall consider the system shown in Fig. 2: the pumping power  $N_{\rm B}$  and the pressure loss to be compensated are given as

$$N_{\rm B} = \dot{V}_{\rm E} \Delta p \tag{28}$$

$$\Delta p = \varrho_{\rm E} g \Delta l \tag{29}$$

The bubble volume fraction at the upper edge of the electrodes,  $\alpha_T$ , is a factor determining the mean voltage drop between the electrodes. Subtracting the mean voltage drop between the electrodes in the absence of bubbles from the aforementioned value, we obtain the voltage increment,  $\Delta U$ , due to the presence of bubbles in the interelectrode gap.

$$\Delta U = \bar{j} d \chi_{\rm E}^{-1} (K_1 - 1 - K_{2\rm B}) \tag{30}$$

The extra power consumed due to the presence of the bubbles in the interelectrode gap,  $N_{\rm E}$ , may be approximated by

$$N_{\rm E} = I_{\rm T} \Delta U \tag{31}$$

If the ratio of the power for pumping the fluid by the gas-lift effect to the extra power is defined as

'pumping efficiency' then this quantity is given by

$$\eta_{\rm P} = \frac{N_{\rm B}}{N_{\rm E}} \times 100 ~(\%)$$
 (32)

The total power consumed in one cell of a bipolar electrolyser,  $N_{\rm T}$ , is given by

$$N_{\rm T} = \bar{\jmath} b l_{\rm E} U \tag{33}$$

#### 3. Experimental details and results

Equation 23 was verified on a pilot scale, undivided electrolyser for water decomposition. To a first approximation, the current efficiencies for H<sub>2</sub> and O<sub>2</sub> evolution,  $\eta_{O_2}$  and  $\eta_{H_2}$ , are set to 1. The electrolyte was 8.77% NaOH solution, the electrode width b = 130 mm, electrode height  $l_E = 703$  mm and interelectrode distance d = 6 mm. The electrolyser was connected to a reservoir of 200 litres, whose outlet was connected to the lower part of the electrolyser. Current collectors were fastened at ten points on the rear faces of the electrolyte level in the reservoir could be changed from + 70 to - 320 mm with respect to the overflow located at the upper edge of the electrodes. The outflowing liquid passed into another reservoir which was provided with a water gauge to measure the flow rate of the electrolyte.

First, the local resistance and pressure losses in the space between the electrodes were measured at a chosen flow rate. The following expression for  $\Delta p_z$  was found:

$$\Delta p_z = 25.7 \,\lambda \varrho_{\rm E} v_{\rm E}^2 \tag{34}$$

Afterwards, the liquid level in the reservoir was set at a chosen height,  $l_{\rm T}$ , and the value of  $\bar{\alpha}$  was calculated from the equation

$$g\varrho_{\rm E}l_{\rm T} - g\varrho_{\rm E}l_{\rm E}(1-\bar{\alpha}) = \left(\lambda_{\rm M}\frac{l_{\rm E}}{d_{\rm E}} + 51.4\ \lambda + 1\right)\frac{1}{2}\,\varrho_{\rm E}\frac{v_{\rm E}^2}{1-\bar{\alpha}}\tag{35}$$

Here, the kinetic energy of the liquid at the inlet is neglected.

The system was not isothermal, since the temperature at the upper edge of the electrodes was always higher than at inlet  $(T_T > T_0)$ . Therefore, the mean dynamic viscosity,  $\mu$ , was calculated according to

$$\mu = \mu_0 \left[ 1 + \frac{1}{2\mu_0} \left( \frac{d\mu}{dT} \right)_{T_0} (T_{\rm T} - T_0) \right]$$
(36)

and the gas volume at the upper edge of the electrodes as

$$\dot{V}_{\rm GT} = \dot{V}_{\rm GT,0} \left( 1 + \frac{T_{\rm T} - T_0}{293} \right)$$
 (37)

In treating the data, the temperature difference between the outflowing and inlet electrolyte was calculated as

$$\Delta T = \left(U - \frac{\Delta H_{298}^0}{2F}\right) \frac{I_{\rm T}}{\dot{V}_{\rm E} \varrho_{\rm E} c_{\rm pE}}$$
(38)

The following physical constants were used:  $\Delta H_{298}^0 = 241.8 \times 10^3 \text{ J}$  for water decomposition [13];  $c_{\text{pE}} = 3789 \text{ J kg}^{-1} \text{ K}^{-1}$  [14];  $\mu_{\text{E}} = 0.00173 \text{ Ns m}^{-2}$  [15];  $\varrho_{\text{E}} = 1095 \text{ kg m}^{-3}$  [16];  $\chi_{\text{E}}^{-1} = 0.03435 \Omega \text{ m}$  [17].

The substantial experimental data are presented in Figs 3, 4 and 5.



Fig. 3. Experimental values of electrolyte flow rate,  $\dot{V}_{\rm E}$  (m<sup>3</sup>s<sup>-1</sup>), versus average current density,  $f(\Lambda \, {\rm cm}^{-2})$ . The dashed line gives the  $\dot{V}_{\rm GT}$ values for different current densities. Values of  $\Delta l$ : ×, 40 mm;  $\triangle$ , 80 mm;  $\Box$ , 160 mm; O, 240 mm; +, 320 mm.

Fig. 4. Experimental values of  $\bar{\alpha}$  as function of average current density,  $\bar{j}$  (A cm<sup>-2</sup>) for different pumping heights. Notation as for Fig. 3



Fig. 5. Total voltage, U(V), on one cell of a bipolar electrolyser versus average current density,  $j(A \text{ cm}^{-2})$  for different pumping heights. Notation as for Fig. 3

#### 4. Discussion

Based on experimental data and Equation 18, the values of  $K_{2B} = 0.408$  and  $(a'_A + a'_C) = 2.16$  V were calculated by the least squares method. The voltage drop of the electrodes and busbars is also included in the value of  $K_{2B}$ . The value 2.16 V for  $(a'_A + a'_C)$  is higher than the thermodynamic value of 1.2 V due to linearization of the U-j relation in the range  $\bar{j} \in \langle 0.005; 0.8 \rangle$  (A cm<sup>-2</sup>). The values of  $\bar{\alpha}$  were then calculated from Equation 23 (for  $v_R = 0$ ) and the same quantities were calculated from the experimental data with the aid of Equation 35.

Numerical integration of Equations 5c and 27 for  $v_{\rm R} = 0$  resulted in values of  $\bar{\alpha}$  higher (on average + 12%) than those obtained by experiment. It was concluded that the bubbles have a certain rising velocity,  $v_{\rm R}$ , resulting in a decrease of the value of  $\alpha_{\rm T}$  and hence  $\bar{\alpha}$ . For each experiment we used Equations 27, 5a and 5c to calculate such a value of  $v_{\rm R}$ , for which the calculated and experimental values of  $\bar{\alpha}$  were identical (see Fig. 6) for  $\alpha_{\infty} = 0.63$ . The  $v_{\rm R}$  values were correlated with superficial gas velocity,  $\dot{V}_{\rm GT}/bd$ ,

$$v_{\rm R} = v_{\rm R}^0 + (0.752 \pm 0.125) \frac{\dot{V}_{\rm GT}}{bd}$$
 (39)

where the upper and lower limits of the mean were calculated from the sample variance, s,

$$s^{2} = \sum (x_{i} - \bar{x})^{2} / (n - 1)$$
(40)

using Student's statistic as  $\pm t(n; 0.05)s/(n)^{\frac{1}{2}}$ . The  $v_{R}^{0}$  value was estimated as  $0.5 \text{ cm s}^{-1}$ . Equation 39 is valid for all experiments up to  $\Delta l = 320 \text{ mm}$ . Equation 39 is only an approximation of a more complicated dependency as can be seen from Fig. 6. The average error of  $v_{R}$  is  $\pm 36\%$ .

With the help of Equation 39 we recalculated the values of  $\bar{\alpha}$ , U,  $U_{\rm B}$ ,  $N_{\rm E}$  and  $N_{\rm T}$  for all experiments (Fig. 7). The calculated values of  $\bar{\alpha}$  are distributed randomly about the experimental values of  $\bar{\alpha}$  with an average error of  $\pm 4.1\%$ . Some of the experimental and calculated data are given in Table 1. The values in Table 1 indicate that the best fit of  $K_{2\rm B}$  using a least squares method for all data predicts lower cell voltage for  $\Delta l = 40$  mm and higher cell voltage for  $\Delta l = 320$  mm, compared to



Fig. 6. Dependence of the calculated  $v_{\rm R}$  (cm s<sup>-1</sup>) values as function of the superficial gas velocity,  $\dot{V}_{GT}/bd$  (cm s<sup>-1</sup>), for the case where experimental  $\bar{\alpha}$  is put equal to calculated  $\bar{\alpha}$ ; ( $\alpha_{\infty} = 0.63$ ). Notation as for Fig. 3

experimental values. The greatest error in total cell voltage is +0.47 V for U = 3.95 V, but this system also results in a very high value of  $\bar{\alpha}$  (Table 1).

The physical background of Equation 39 lies, according to Hine [8], in the dependency of  $v_{\rm R}$  (or the bubble diameter) on the superficial gas velocity. Equation 2f can be used for the evaluation of experimental data for systems where 'channelling' of bubbles takes place. The rising velocity,  $v_{\rm R}$ , calculated according to Stokes law is considerably smaller than the value calculated from Equation

$\Delta l (mm)$	$\overline{j} (A cm^{-2})$	U (V)	U(V)	ā	ā
		(experimental)	(theory)	(experimental)	(theory)
40	0.055	2.40	2.33	0.0701	0.0695
40	0.109	2.56	2.50	0.0789	0.0754
40	0.172	2.80	2.71	0.0860	0.0872
40	0.219	2.98	2.86	0.0912	0.0941
40	0.268	3.15	3.03	0.0979	0.0979
40	0.312	3.25	3.17	0.1042	0.1005
40	0.438	3.80	3.62	0.1125	0.1213
40	0.547	4.30	4.01	0.1295	0.1299
40	0.648	4.80	4.52	0.1353	0.1465
40	0.793	5.30	4.94	0.1446	0.1566
320	0.328	3.95	4.42	0.4728	0.5179
320	0.438	4.60	4.91	0.4841	0.4854
320	0.547	5.20	5.64	0.4912	0.4905
320	0.640	5.80	6.23	0.4976	0.4910
320	0.766	6.60	6.90	0.5150	0.4800

Table 1. Experimental and calculated values for  $\Delta 1 = 40 \text{ mm}$  and  $\Delta 1 = 320 \text{ mm}$ 



Fig. 7. Power consumed for electrolysis in one cell  $(N_{\rm T})$ , 'extra-power' consumed due to the presence of gas bubbles in the electrolyte  $(N_{\rm E})$  and power required for pumping due to the gas-lift effect  $(N_{\rm B})$  as functions of the average current density,  $\bar{\jmath}$ , for two pumping heights. Open symbols:  $\Delta l = 40$  mm; solid symbols:  $\Delta l = 320$  mm.  $N_{\rm T}$ ,  $\odot \oplus$ ;  $N_{\rm E}$ ,  $\Delta \in$ ;  $N_{\rm R}$ ,  $\Box = 1$ .

39. This opinion supports the values published for a pilot plant electrolyser for chlorate production [18], with b = 148 mm, d = 9 mm and  $l_{\rm E} = 700 \text{ mm}$ . For evaluation of the data it was necessary to use unusually high rising velocities based on estimated bubble diameters (0.036–0.048 cm), because the experimental data indicated very low  $\bar{\alpha}$  values. The experimentally measured bubble diameters were only 0.018–0.024 cm.

As a result, Equation 39 can be recommended for a system with  $d \approx 6 \text{ mm}$  and also for systems with recirculation of the electrolyte described in Fig. 1.

The 'pumping efficiency' was, in our system, in the range 0.01 to 3.5%. Nevertheless, the simplicity of pumping and the very low absolute values of power needed for pumping ( $N_E$ ) compared to the total power input ( $N_T$ ) make it feasible to use the bubbles for pumping (electrolyte circulation) in closed loops.

#### 5. Conclusions

Equation 35, giving the volume fraction of bubbles,  $\bar{\alpha}$ , was verified experimentally on a pilot scale electrolyser. In the interelectrode gap the velocity of rising bubbles,  $v_R$ , is co-determined by the superficial gas velocity Equation 39 and by the flow of bubbles in 'channels' (in the swarm in the vicinity of the electrode) and therefore  $v_G$  can be approximated by Equation 2f. Equations 39 and 2f are also important in calculating the circulation rate or the pumping height for industrial electrolysers used in the production of hydrogen, oxygen or chlorates. Equation 39 represents a

correction (4/20%) to be used in the calculation of  $\bar{\alpha}$  or related quantities, e.g.  $\chi_E/\chi_M$ , in which the Stokes velocity of bubbles is put equal to zero ( $v_R = 0$ ).

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